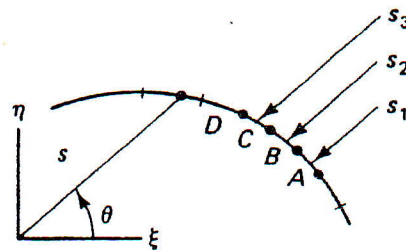


**Answer all the following questions:**

- 1-1) What are the elements and kinds of mechanisms?  
 1-2) The kinematic constraints of a four-bar mechanism are:  $2\cos\theta_1 + 4\cos\theta_2 - 3\cos\theta_3 = 3.5$ ,  
 $2\sin\theta_1 + 4\sin\theta_2 - 3\sin\theta_3 = 1$ . If the initial angular displacement of the crank is  $\theta_1^0 = 2.36$  rad,  
 and its constant angular velocity is  $2\pi$  rad/sec and  $\theta_2 = 0.57$  rad. Determine the initial  
 angular velocity and the initial angular acceleration of each body of the mechanism.

- 2-1) Classify the kinematic pairs and illustrate six examples.  
 2-2) The curve of a cam follower is descritized and a porsion of the recorded data is listed  
 as shown in the figure.

Point	$\theta$ (rad)	$s$ (cm)
.	.	.
.	.	.
.	.	.
A	0.2	3.75
B	0.3	3.57
C	0.4	3.35
D	0.5	3.10
.	.	.
.	.	.
.	.	.



A spline function algorithm finds three cubic polynomials for three segments of the curve:

$$s_1 = -6.538\theta^3 + 3.230\theta^2 - 2.173\theta + 4.108 \quad \text{cm}$$

$$s_2 = 6.538\theta^3 - 8.538\theta^2 + 1.358\theta + 3.755 \quad \text{cm}$$

$$s_3 = -9.515\theta^3 + 10.846\theta^2 - 6.396\theta + 4.788 \quad \text{cm}$$

Show that  $s_1$  and  $s_2$  and their first derivatives are contiouous at point B. Determine the slope of tangent ( $dn/d\xi$ ) at the point P ahere  $\theta^P = 0.26$  rad

3-1) What are the four basic types of motion in solid mechanics, illustrate some examples.

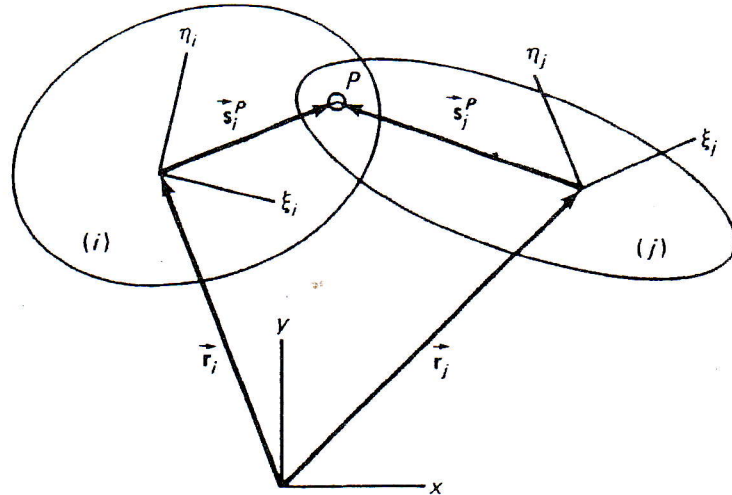
3-2) Consider the shown system of two moving bodies connected by a revolute joint. The external forces acting on the system are gravity, a constant force of 10N acting on body i in the negative x dierction, and a constant force of 10N acting on body j in the positive x direction. The vectors of coordinates, velocities, and accelerations are:

$$\mathbf{q}_i = [1.58, 1.59, 0.6]^T, \quad \mathbf{q}_j = [3.4, 1.96, 0.2]^T,$$

$$\dot{\mathbf{q}}_i = [1.1, 0.2, -0.02]^T, \quad \dot{\mathbf{q}}_j = [1.14, 0.24, 0.03]^T,$$

The linear acceleration components of body i are:  $\ddot{x} = 1.1 \text{ m/sec}^2$  and  $\ddot{y} = 0.2 \text{ m/sec}^2$ , and the constant quantities of this system are:  $m_i = 1.2 \text{ kg}$ ,  $m_j = 2 \text{ kg}$ ,  $\mu_i = 2.5 \text{ kgm}^2$ ,  $\mu_j = 4 \text{ kgm}^2$ ,





- i) Calculate the number of degrees of freedom of the system.
- ii) Calculate the joint reaction forces at the instant.
- iii) Calculate the angular acceleration  $\ddot{\phi}_i$  and the acceleration vector  $\ddot{\mathbf{q}}_j = [\ddot{x}, \ddot{y}, \ddot{\phi}]^T$
- iv) Check your results.
- v) Express the equations of motion of the system in matrix form.

4-1) Define the types of constraints and explain their differences.

4-2) Consider the classical problem of a circular disk D with radius  $R = \sqrt{14}$  cm rolling on a rough flat horizontal surface S. Let  $P(x_p, y_p, z_p)$  be the point of contact between D and S, where:  $x_p = 0.5t^2$  sec,  $y_p = -0.5t$  sec, and let  $C(x_c, y_c, z_c)$  be the center of mass of D where  $z_c = 0.75t^2$  sec. Let x, y and z be coordinate axes fixed on S with origin o and with z being vertical, and let  $\xi, \eta$  and  $\zeta$  be the moving coordinates fixed on D with origin C. Where the rotational transformation matrix of the coordinate systems is given by the matrix

$$A = \begin{bmatrix} 0.3 & 0.2 & -0.7 \\ 0.2 & 0.5 & -0.4 \\ -0.7 & -0.4 & 0.6 \end{bmatrix}, \text{ (a) Deduce the components of the vector } \rho \text{ from C to P and the}$$

position vector  $\mathbf{r}$  from o to C at  $t=2$ sec. (b) Show that the rolling disk with no slipping condition is considered a non-holonomic constraint, while the rolling with longitudinal slipping is considered as a holonomic constraint.

5-1) Define the differences between a special purpose computer program and a general purpose computer program. What are four major tasks that must be performed by the general-purpose computer program for the dynamic analysis of multibody systems?

5-2) Write down the meanings of the following abbreviations CAE, CAM, CAD, CAP, DAP, ADAMS, MBOSS, DADS.